

Insights into the structural, electronic and magnetic properties of gold clusters: Comparison between Au_{12}Cr and Au_{12}Mo clusters

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Abstract. Modification of the chemical and physical properties with respect to element components in atomic clusters has opened up significant potential in both fundamental study and applications. In this work, we theoretically investigate the structure, stability, and magnetic properties of gold clusters doped by Cr and Mo (Au_{12}Cr and Au_{12}Mo) using the density functional theory calculation. The bond strength of AuM dimers dictates the globally minimum structural evolution in the Au_{12}M clusters, which can be classified into two principal forms: the icosahedral (Mo dopant) and the cone-like structures (Cr dopant). The average binding and dissociation energies results indicate that the enhanced stability of cluster stems from the contribution of Cr/Mo atom. However, their magnetic moments are entirely distinct. To gain insight and a better understanding of the electronic configuration and magnetic behavior of the study clusters, the molecular orbital diagram and the spin distribution are computed. The Au_{12}Cr cluster exhibits a significant magnetic moment of $4 \mu_B$, whereas the magnetic moment is completely quenched in the Au_{12}Mo cluster. Furthermore, the infrared IR spectrum of Au_{12}M is also predicted.

Keywords: Au_{12}Cr , Au_{12}Mo clusters; density functional theory; magnetic moment.

Classification numbers: 31.15.xv; 31.15.E-; 75.30.-m; 81.07.-b.

1. Introduction

Much attention has been dedicated to gold clusters in the recent decades thanks to their intriguing chemico-physical characteristics, such as magnetism, optics, catalysis, and electronic behavior, with a great potential in nanotechnology, electronics, and materials science [1–7]. Both theoretical and experimental investigations have revealed that the composition, shape, size, and charge state of the gold clusters have been considered as key factors for modifying their properties. Pure clusters behave as a non-magnetic material, while the appearance of the transition metal atom triggers the magnetic state in the cluster [8–10]. The unfilled $3d$ electrons of the transition metal dopant atoms have been demonstrated to play a crucial role in the unusual stability and distinctive properties of doped gold clusters. The hybridization between the s -delocalized electrons of the host and d -localized electrons of dopant atoms generates different electronic structures, resulting in a significant effect on the geometric structure and characteristics. Yang and colleagues [11] indicated the close correlation between the geometric, electronic structure and magnetic properties of Au_{24}M clusters ($\text{M} = \text{V-Ni}$), as well as the valence electron configuration of the transition metal atom. The electronic structure based on a confined electron gas in a spherical structure complied with the jellium model was proposed by Knight et al. [12], forming cage-like structures with a large magnetic of $3 \mu_{\text{B}}$ to $6 \mu_{\text{B}}$. In this instance, the $3d$ transition metal atoms preferentially occupy positions with higher coordination numbers, typically located at the center of the cage. The effect of hybridization between valence electrons of the vanadium atom and those of noble clusters (Au_n , Ag_n , and Cu_n) has been found to play a significant role in stability and magnetic properties [13, 14]. On the other hand, the electronic structure evolution of the Au_{19}M ($\text{M} = \text{Sc-Ni}$) clusters has been explained by Tam and colleagues to follow the $1\text{S}^2 1\text{P}^6 1\text{D}^{10}$ filling rule [15, 16]. This suggests that the geometric structure of the Au_{19}M clusters grows in accordance with a highly symmetric tetrahedral pyramid shape. The Au_{19}Cr cluster is utterly stable and high magnetic moment of $5 \mu_{\text{B}}$. A similar picture is also observed in Au_9M^{2+} ($\text{M} = \text{Sc-Ni}$) clusters [17]. The remarkable influence of the position Fe atom on the electronic structure and magnetization of Au_{18}Fe and Au_{19}Fe clusters has been the subject of intensive investigation by Ehlert [18].

It is noticed that the $4d$ transition metal atoms exhibit more stable and filled electron configurations in various energy levels, stabilities, oxidation states, and chemical properties than the $3d$ transition metal atoms. When the group $3d$ and $4d$ atoms are attended in the gold clusters, their electronic structure differences result in distinct bonding patterns, spatial arrangements, and structural motifs [19]. The endohedral gold clusters containing ten gold atoms Au_{10}W with large HOMO-LUMO gap, high ionization potential and electron affinities suggest that these clusters are all likely to be stable chemically, which is similar to the super-halogen Al_{13} [20]. The existence of icosahedral 18-electron clusters Au_{12}W was predicted theoretically [21] and found experimentally [22]. Anionic icosahedral 18-electron clusters $\text{Au}_{12}\text{Ta}^-$ and $\text{Au}_{12}\text{Re}^+$ were predicted theoretically [22]. These are explained by the hybridization of 1S , 1P , and 1D molecular orbitals in dopant nanoclusters. There is a contribution from the 12 valence electrons of the $6s$ -Au and six valence electrons from the dopant atoms. Juarez. L. F. Da Silva et al. [23] shown different trends in the structure and electronics of the $3d$ and $4d$ metal clusters containing 13 atoms by an effective coordination increase in large d state occupation. This comparative study provides insight into how the occupation of the d states influences the structural and electronic characteristics of these bimetallic systems.

It can be observed that gold clusters doped a transition metal atom provides opportunities to combine diverse geometric structures and unique properties of clusters with different electronic configurations. Therefore, this work investigates and compares the electronic, geometric structure, and IR spectra of the lowest energy state Au_{12}M ($\text{M} = \text{Cr}$ and Mo) clusters using density functional theory (DFT) calculations. Surprisingly, we have found two contrasting characteristics in the behavior of doped transition metal atom in gold clusters. The magnetism of the doped $4d$ transition metal atom cluster is completely quenched, resembling the Kondo effects. Conversely, the doped clusters of $3d$ atoms exhibit a significant magnetic moment. The magnetic moment of dopant clusters is correlated with the d -state electron of transition metal atoms. These theoretical findings provide important insight into advanced nanomaterials as foundational knowledge for upcoming experimental investigations.

2. Computational method

The geometric and electronic structures of Au_{12}M ($\text{M} = \text{Cr}$ and Mo) clusters were carried out by DFT calculations in the Gaussian 09 package [24, 25]. In this study, the initial optimization of the guessed structures involved the usage of the TPSS functional combined with basis set of cc-pVDZ-pp for Au and cc-pVDZ for Cr/Mo atoms, respectively. The isomers with relative energies below 2.0 eV were considered for further calculations. These selected isomers underwent single-point energies calculations using the same functional, but combining with larger basis sets, including cc-pVTZ-pp for Au and cc-pVTZ for Cr/Mo atoms, which based on previous investigations [26]. The functional selection is also based on test calculations for Au_2 , AuCr , and AuMo dimers. These calculated results are presented in Table 1, along with available computational and experimental data for comparison. A self-consistent approach was employed with the convergence criteria of 2×10^{-5} Hartree for energy and 5.0×10^{-3} Å for displacement. The optimization calculations were followed by frequent calculations to identify the cluster's energy-minimized structure. The electronic configurations of ground-state clusters Au_{12}M ($\text{M} = \text{Cr}$ and Mo) were explored by using molecular diagram (MO) and spin density. The total/local magnetic moments (TMMs/LMMs) were defined as the difference between the numbers of spin-up and spin-down electrons occupying the molecular/atomic orbitals of the cluster/atom.

Table 1. Theoretical and experimental results of bond length R_e (Å) and dissociation energy D_e (eV) for Au_2 , AuCr , and AuMo clusters.

Clusters		TPSS	TPSS	PBEPBE	BP86	Expt./others calculation
Au_2	R_e	2.51		2.52	2.52	2.47
	D_e	2.28		2.29	2.27	2.29 ± 0.008 [27]
AuCr	R_e	2.46		2.47	2.46	
	D_e	2.26		2.23	2.35	2.29 ± 0.30 [27]
AuMo	R_e	2.54		2.54	2.58	2.55 [28]
	D_e	2.27		2.28	2.29	2.26 [28]

3. Results and discussion

3.1. The optimal geometric and spin multiplicities

The effects of $3d$ and $4d$ transition metal atoms on pure gold clusters Au_{13} were investigated by means of the optimization process of geometrical and electronic structures. Firstly, the Au_{13} cluster was computed to find the most stable geometric structure. Next step is the replacement of an Au atom in the Au_{13} cluster by a Cr or Mo atom at all feasible positions to generate initial Au_{12}M structures for the optimization calculations. Noticeably, there are several low-lying isomers and corresponding spin configurations for each Au_{12}M ($\text{M} = \text{Cr}$ and Mo), which satisfies convergent condition. Nevertheless, only the structures with lowest energy considered as the ground-state configuration are discussed. They are displayed in Fig. 1 for both Au_{12}Cr and Au_{12}Mo clusters. Comparing to previous articles, our calculations results are in a complete agreement with those published findings [29]. In the following, the isomers with increasing order of energy are donated as A, B, and C. Additionally, information regarding the spin multiplicities and energy differences compared to each ground-state structure is also presented.

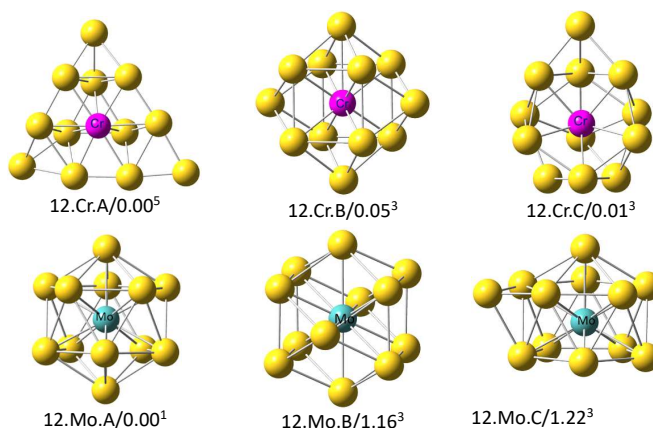


Fig. 1. Optimized structures, spin multiplicities, and relative energies (in eV) of the lowest lying isomers of Au_{12}M ($\text{M} = \text{Cr}$ and Mo). The yellow, magenta, and blue balls show Au, Cr and Mo atom, respectively.

The significant difference in geometric structure and spin multiplicities is observed in the gold clusters, corresponding to $3d$ (Cr) and $4d$ (Mo) transition metal dopants. The $\text{Au}_{12}\text{Mo.A}$ cluster shows the perfect icosahedral cage structure with singlet spin, while the $\text{Au}_{12}\text{Cr.A}$ has a cone-like structure and higher spin of quintet, which can be attributed to Jahn-Teller effects. Structural rearrangement occurred at different isomers corresponding to higher energies. In addition to the change of geometry from the cone-like shape ($\text{Au}_{12}\text{Cr.A}$) to dodecahedral structure ($\text{Au}_{12}\text{Cr.B}$), the Cr atom moves from the face to the center of the frame. The difference in energy between $\text{Au}_{12}\text{Cr.B}$ and the ground-state $\text{Au}_{12}\text{Cr.A}$ is 0.05 eV. The relative energy of the unstable triplet $\text{Au}_{12}\text{Cr.C}$ is higher than the ground-state by 0.1 eV, and the geometry again tends to retain a layered motif with a substituted dopant atom on the surface center. At this energy, the pin-like structure in bowling game is grown in the $\text{Au}_{12}\text{Mo.C}$. Conversely, higher relative energy levels are

required to evolve the $\text{Au}_{12}\text{Mo.B}$ and $\text{Au}_{12}\text{Mo.C}$ structures. The transformation from the high-symmetry icosahedral to hexagonal-like structure according to the energy difference of 1.16 eV or to more complex polygonal shape in the least unstable cluster (the energy difference of 1.22 eV) is observed. However, the central position of Mo dopant atom is preserved in three configurations.

The difference in the shape of Au_{12}M ($\text{M} = \text{Cr}$ and Mo) can be explained by the differences in the binding energy (BE) of AuM and Au_2 . The calculations point out that the Au-Mo (1.15 eV) bond is stronger than that of Au-Au (1.13 eV), this value is similar in the case of Au-Cr (1.13 eV). This confirmed that the Mo atom favors the high position compared with Cr atoms. A similar behavior was reported for Ag_{12}Cr in the previous studies [29, 30]. In that system, the binding energy (BE) of Ag-Ag bonds (0.81 eV) is higher than the BE of Ag-Cr bonds (0.73 eV). As a result of this difference in the binding energies, the Cr atom is substituted by an Ag atom in the central icosahedral structure.

3.2. Stabilities

To evaluate how the transition metal dopant atom affects the stability of the clusters, the average BE is calculated and then compared to that of the pure gold clusters Au_{13} . The BE values are determined by the following formulas:

$$BE(\text{Au}_{12}\text{M}) = \frac{1}{13}[E(\text{M}) + 12E(\text{Au}) - E(\text{Au}_{12}\text{M})], \quad (1)$$

$$BE(\text{Au}_{13}) = \frac{1}{13}[13E(\text{Au}) - E(\text{Au}_{13})], \quad (2)$$

where $E(\text{M})$, $E(\text{Au})$, $E(\text{Au}_{13})$, and $E(\text{Au}_{12}\text{M})$ correspond the total energies of M, Au atoms, and the Au_{13} , Au_{12}M clusters. Visibly, the binding energy values of doped clusters are significantly higher than the BE of pure counterpart, BE (Au_{12}Cr) of 2.24 eV and BE (Au_{12}Mo) of 2.49 eV compared to BE (Au_{13}) of 2.0 eV, as shown in Table 1. It can be concluded that the role of Cr and Mo atoms enhance the stability of Au clusters. An analogous picture was also obtained for Au_9M^{2+} ($\text{M} = \text{Sc-Ni}$) clusters [17] in which the estimated atomic-averaged binding energy of the most stable $\text{Au}_9\text{Cr}^{2+}$ was substantially higher than that of Au_{10}^{2+} cluster. This trend is also observed in gold clusters doped 4d transition metal atoms Au_{n-1}Y . The global structure with the Y atom has the highest number of neighboring Au atoms because the Au-Y bond strength is stronger than that of the Au-Au bond [31].

Table 2. The binding energy per atom (BE in eV), dissociation energies (DE in eV), and bond length ($R_{\text{M-Au}}$ in Å) of Au_{13} and Au_{12}M clusters.

Clusters	BE (eV)	DE (eV)	
		loss Au	loss M
Au_{13}	2.0	1.75	-
Au_{12}Cr	2.24	2.75	3.13
Au_{12}Mo	2.49	4.83	6.56

Furthermore, we also consider dissociation energies (DE in eV) in order to understand the influence of the M atom on the thermodynamic stability of Au_{12}M ($\text{M} = \text{Cr}$ and Mo) structure.

The fragmentation of Au_{12}M cluster via two major possible channels was calculated, including a loss of a M atom, and an Au atom. The formulas for calculating the DE are expressed as follows:

$$\text{DE}(\text{M}) = E(\text{Au}_{12}) + E(\text{M}) - E(\text{Au}_{12}\text{M}), \quad (3)$$

$$\text{DE}(\text{Au}) = E(\text{Au}_{11}\text{M}) + E(\text{Au}) - E(\text{Au}_{12}\text{M}), \quad (4)$$

where E represents the energy of the atom/cluster. The dissociation energies are presented in the Table 2 as well, which are defined as the energetic difference between the total electronic energies of the species generated in each dissociation channel and the electronic energies of the parent clusters. Obviously, the loss of an Au atom is the most energetically preferred dissociation channel, whereas the other channel to decay a M atom requires a higher energy. Compared to Au_{12}Cr , the dissociation energies of both channels in the Au_{12}Mo are significantly higher, indicating more stable Au_{12}Mo structure. This result is very consistent with the average binding energy.

3.3. Electronic and magnetic properties

As well known, Cr and Mo are strong magnetic elements with outermost atomic shell of $3d^5 4s^1$ and $4d^5 5s^1$, respectively. However, doping Cr or Mo atoms into gold clusters results in a completely different scenario. Typically, the magnetism in Au_{12}Mo is entirely quenched, yet the Au_{12}Cr cluster shows non-zero magnetic state of $4 \mu_B$. In this regard, our objective is to investigate the fundamental physics to explain the distinction between these clusters. Additionally, determination whether if the possibility to develop a universal mechanism for predicting the magnetic behavior in analogous quantum systems is a fascinating finding. It is worth mentioning that substituting different transition metal impurity atoms while maintaining the host clusters intact results in different significant variations of properties in the dopant systems. Particularly, the lowest-lying isomer of Au_{12}Cr favor in the cone shape, whereas Au_{12}Mo is icosahedral cage for comparison, as mentioned above. As a consequence, their electronic configurations display a remarkable difference [32–34]. The electronic shell structure formation in these clusters can be explained by the interactions between the delocalized (*s*) and localized (*d*) electrons. It assumes that each gold atom delocalizes its $6s^1$ electron, while the Cr and Mo atoms collectively contribute 6 valence electrons from the configurations of $3d^5 4s^1$ and $4d^5 5s^1$, respectively. As a result, the Au_{12}Cr and Au_{12}Mo will provide a total of 18 valence electrons. A graphical representation of their corresponding molecular orbital diagram was plotted to get more clear clarity on the electronic shell structure of the clusters, as seen in Fig 2. By examining the molecular orbitals (MOs) and their orbital energy levels for the Au_{12}Cr and Au_{12}Mo , it can be observed significant differences, which serve as an indicator of distinct variations in their electronic thermochemical stability. In the case of the Au_{12}Mo cluster, there is strong hybridization of $6s$ orbital of Au and the *sd* orbitals of Mo, leading to the delocalization of all six valence electrons of Mo ($4d^5 5s^1$), which then combine with twelve *s* valence electrons of the Au host. This process results in the complete filling of the $1S^2 1P^6 1D^{10}$ orbitals, forming a closed shell configuration and a stable structure. Consequently, the Mo dopant exhibits a quenched magnetic moment. In analogy to Cu_{12}Cr , Mai and et al., have observed the completely magnetic quenching in the Cu_{12}Cr which the valence electrons fulfill the 18-electrons counting rule ($3d^5 4s^1$) for Cr atom and twelve $5s^1$ electrons for copper atoms [29].

On the other hand, only two delocalized electrons of $4s$ -Cr join in twelve electrons of the Au host cluster, forming electronic shell structure of $1S^2 1P^6 1D^6$. The remaining 4 electrons are localized on $3d$ -Cr atomic orbitals, responding to the magnetic properties. The magnetic moment

of Au_{12}Cr , therefore, originated from the co-existence of delocalized electron shell and localized magnetic shell. It turns out that the electronic configuration of the Au_{12}Mo and Au_{12}Cr clusters basically satisfies the electronic shell model of $1\text{S}^21\text{P}^61\text{D}^{10}$ and $1\text{S}^21\text{P}^61\text{D}^63\text{d}^4_{\uparrow}$ with completely quenched and $4 \mu_{\text{B}}$ magnetic moments, respectively.

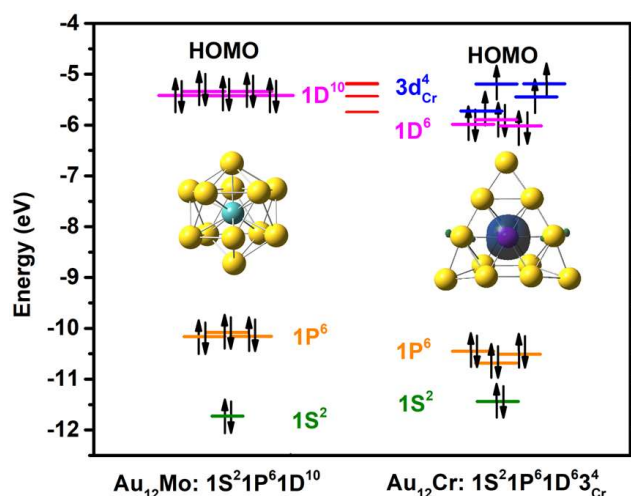


Fig. 2. The MO diagram of Au_{12}Mo (left) and Au_{12}Cr (right) clusters.

It can be seen that the magnetism of Au_{12}Mo and Au_{12}Cr depends on the hybridization of $3d$ dopant electrons and s host electron. To understand more about the magnetic properties of studied clusters, we analyzed the local magnetic moment (LMM) and total magnetic moments (TMM) in μ_{B} . The magnetic moment of $3d/4d$ -M ($M = \text{Cr}$ and Mo), $6s$ -Au and total magnetic moment (in μ_{B}) of Au_{12}M are shown in Table 3. Regarding the Au_{12}Mo , the $4d$ local magnetic moment of Mo and $6s$ of Au is zero. This result aligns with the molecular orbital diagram, which indicates the pairing of Mo and Au valence electrons within the molecular shell. Compared with the Au_{12}Mo , the Au_{12}Cr is more interesting. The LMM in the $3d$ orbitals of Cr is $3.6 \mu_{\text{B}}$, while that of $6s$ orbital of Au is only $0.01 \mu_{\text{B}}$. In other words, the TMM of clusters is predominantly contributed by the LMM of $3d$ -atom.

Table 3. Local magnetic moments (LMM in μ_{B}) of Cr/Mo atom, and total magnetic moment (TMM in μ_{B}) of Au_{12}Cr and Au_{12}Mo , respectively.

Au_{12}M	LMM (μ_{B})				TMM (μ_{B})
	$3d/4d - M$	$4s/5s - M$	$4p/5p - M$	$6s - \text{Au}$	
Au_{12}Cr	3.60	0.03	0.04	0.01	4
Au_{12}Mo	0	0	0	0	0

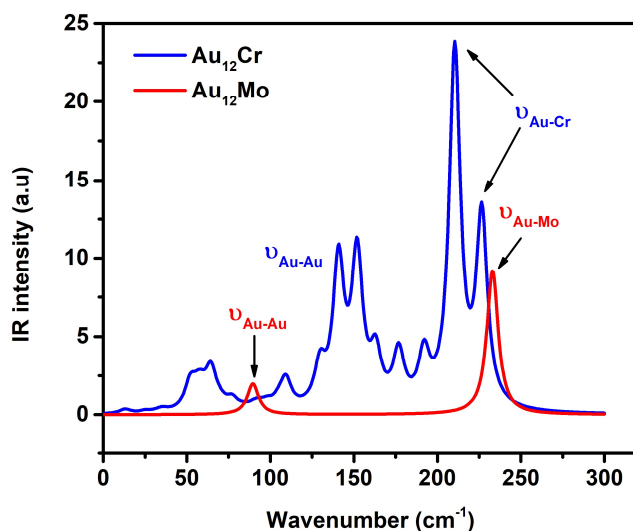


Fig. 3. IR spectra for Au₁₂M (M = Cr and Mo) clusters. The blue and red curves represent the IR spectrum of Au₁₂Cr and Au₁₂Mo clusters, respectively.

3.4. IR spectra of the investigated clusters

In this subsection, we investigate the IR spectra of the most stable structure. The infrared IR spectrum provides valuable information and insight into molecular structure and vibrational modes. Theoretical research results on IR spectra play a crucial role in advancing further studies, especially in experimental investigations, assisting in the accurate determination of cluster structures during synthesis. However, no information about the infrared IR spectrum of Au₁₂M clusters has been reported both experimentally and theoretically so far. Therefore, the IR spectra of Au₁₂M (M = Cr and Mo) are regarded as a first fingerprint for identifying the cluster with respect to the geometrical structure and composition of M atoms. For the purpose of comparison in order to help distinguish the two dopant atoms, Au₁₂Cr and Au₁₂Mo clusters, the calculated IR spectra. Fig. 3 displays the IR spectra of Au₁₂Cr and Au₁₂Mo with the range from 0 to 300 cm⁻¹ because no detectable signals were observed at higher photon energy levels. The peaks corresponding to higher frequencies (> 210 cm⁻¹) are represented the vibrations of the Cr/Mo atoms within the Au₁₂ host framework, while the lower frequency peaks characterize the vibration of Au-Au bonds. This picture shows good agreement for the neutral dimer Au-Au vibration at a frequency of 190.0 cm⁻¹ [35]. According to the IR spectra and experimental findings, the vibration Au₁₂ is also observed at frequency of less than 200 cm⁻¹ [36]. As can be seen in Fig 3, the vibrational spectra in the icosahedral Au₁₂Mo structure only exhibits two high intense peaks. The highest peak, located at ~234 cm⁻¹ is characteristic of the symmetric stretching mode of Mo-Au bonds. The lower peak at ~91 cm⁻¹ corresponds to the symmetric stretching vibrations of Au-Au bonds. In other words, the lowest-lying structure of Au₁₂Mo clusters is utterly high symmetry with icosahedral shape. In contrast to the IR spectra of the Au₁₂Mo, the IR spectra of Au₁₂Cr cluster is more complicated, characterized by multiple peaks. Considering the distorted cone shaped Au₁₂Cr spectrum, it can be observed two asymmetric stretching modes of Cr-Au bonds at high frequencies: ~210 cm⁻¹

and $\sim 227\text{ cm}^{-1}$. The peaks at $\sim 110\text{ cm}^{-1}$, $\sim 141\text{ cm}^{-1}$ and $\sim 163\text{ cm}^{-1}$ are assigned to the symmetric stretching of Au-Au bonds. Conversely, the asymmetric stretching modes of Au-Au bonds are assigned at $\sim 64\text{ cm}^{-1}$, $\sim 110\text{ cm}^{-1}$, $\sim 130\text{ cm}^{-1}$, $\sim 152\text{ cm}^{-1}$ and $\sim 177\text{ cm}^{-1}$.

4. Conclusion

The geometric and electronic structures, stability, and magnetic properties of the 13-atom gold cluster doped with 3d and 4d transition metal atoms, Au_{12}M with $\text{M} = \text{Cr}$ and Mo were investigated using DFT methods. The most stable isomer of Au_{12}Cr favors a cone-like shape, and the Au_{12}Mo structure prefers an icosahedral structure with Mo located in the center. The electronic shell of Au_{12}Mo is filled with a magic number of 18 valence electrons, which has a perfect icosahedral structure, and enjoy enhanced stability with high binding and dissociation energies. Their higher stability can be interpreted in terms of the electronic shells of the jellium model. The magnetic moment of the clusters has been demonstrated to be proportional to the number of unpaired electrons that are localized on the 3d-M orbitals. This finding opens up an avenue for how chemically inert gold clusters can be adjusted magnetically by a suitable transition metal impurity. The IR spectra of Au_{12}M are simulated to provide valuable guidance for future experimental assignments of these ground-state bimetallic systems.

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Conflict of interest

The authors have no conflicts of interest to declare.

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